

## Class 10-Mathematics

**Instructions for students: The notes provided must be copied to the Maths copy and then do the homework in the same copy.**

### Chapter 15

#### Circles

##### Angle properties of circles

**Theorem 1:** The angle subtended by an arc of a circle at the centre is double the angle subtended by it at any point on the remaining part of the circle.

**Theorem 2:** Angles in the same segment of a circle are equal.

**Theorem 3**(Converse of theorem 2): If a line segment joining two points subtends equal angles at two other points lying on the same side of the line containing the line segment, then the four points lie on the same circle. (i.e. they are concyclic)

**Theorem 4:** Angle in a semicircle is a right angle.

**Theorem 5**(Converse of theorem 4): If an arc of a circle subtends right angle at any point on the remaining part of a circle, then the arc is a semicircle.

Exercise 15.1(Refer the diagrams from textbook carefully and solve the problems)

$$1. \text{ v) } \angle DPD = 180 - 120 = 60^\circ \text{ (Linear pair)}$$

$$\angle ABD = 70^\circ \text{ (Angles in the same segment)}$$

$$x = 180 - (\angle DPD + \angle ABD) \text{ (Angle sum property)}$$

$$= 180 - (60 + 70) = 50^\circ$$

$$3. \text{ b) Reflex } \angle AOC = 360 - 130$$

$$= 230^\circ = 2 \angle ABC \text{ (The angle subtended at the centre is double the angle subtended on the remaining part of the circle)}$$

$$\angle ABC = \frac{230}{2} = 115^\circ$$

$$5. \text{ b) Reflex } \angle AOB = 360 - 140$$

$$= 220^\circ$$

$$\angle ACB = \frac{220}{2} = 110^\circ \text{ (The angle subtended at the centre is double the angle subtended on the remaining part of the circle)}$$

$$\begin{aligned}\angle OBC &= 360 - (\angle OAC + \angle AOB + \angle ACB) \\ &= 360^\circ - (50^\circ + 140^\circ + 110^\circ) \\ &= 360 - 300 = 60^\circ\end{aligned}$$

Now, Join AB

$$\begin{aligned}\angle OAB = \angle OBA &= \frac{180-140}{2} \text{ (OA = OB, property of isosceles triangle.)} \\ &= 20^\circ\end{aligned}$$

$$\begin{aligned}\angle CBA &= \angle OBC - \angle OBA \\ &= 60^\circ - 20^\circ = 40^\circ\end{aligned}$$

$$\begin{aligned}\text{Ans. i) } \angle ACB &= 110^\circ & \text{ii) } \angle OBC &= 60^\circ \\ \text{iii) } \angle OAB &= 20^\circ & \text{iv) } \angle CBA &= 40^\circ\end{aligned}$$

$$\begin{aligned}20. \text{ b) i) To prove } \angle PAD &= \angle PCB \\ \angle BAD &= \angle BCD \dots \text{(i)} & \text{(Angles in the same segment)} \\ \angle PAD &= 180 - \angle BAD \dots \text{(ii)} \\ \angle PCB &= 180 - \angle BCD \dots \text{(iii)} \\ \therefore \angle PAD &= \angle PCB & \text{(From i, ii and iii)}\end{aligned}$$

Hence proved.

ii) To prove  $PA \times PB = PC \times PD$

In  $\triangle PBC$  and  $\triangle PDA$

$$\begin{aligned}\angle PBC &= \angle PDA \text{ (Angles in the same segment)} \\ \angle PCB &= \angle PAD \text{ (From the statement proved above)}\end{aligned}$$

$$\triangle PBC \sim \triangle PDA \quad \text{(AA criteria of similarity)}$$

$$\frac{PB}{PC} = \frac{PD}{PA} \text{ (Property of similar } \Delta\text{s)}$$

$$\Rightarrow PA \times PB = PC \times PD \quad \text{Hence proved.}$$

### Home Work:

- Solve **Exercise 15.1 Questions 4, 5, 7, 8, 10, 15 and 19** in the Maths copy.
- Practise all questions from exercise 15.1